

ARTS1120

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 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'hc'FYgdYWM\cong \cong m5W_bck``YX[Y'h\Y'HfUX]hjcbU``7i ghcX]Ubgž h\Y'6YXY[U'`fPYbg]b[hcb'WUadigŁz'; UX][U'`fP]hmUbX'5fh\/\'8Yg][b'7UadigYgŁ'UbX'h\Y'B[i bbUkU`dYcd'Y'fbi ghfU`]Ub'8YZYbW'': cfW''5WUXYam]b'7UbVYffUŁ'cZh\Y'`UbXg'k\YfY'YUW\'WUadig'cZI BGK ']g`cWJhYX''$

7ci fgY 8YHJ] g

7 fYX]hDc]bhg * *

Gi a a UfmcZh\Y 7ci fgY

8 c mci 'k Ubhihc 'gYY' dYfZcfa UbW' `]j Y'cb 'ghU[Y3'8 c mci 'k Ubhihc 'Z]bX'ci h\ck ']hg'a UXY3'A UmVY' mci 'j Y VYYb'a cj YX'VmUb'UWcf'g'dYfZcfa UbW'žUa UnYX'Vmih\Y'VYUi hmcZUb']a U[Y'cf'WUi [\hU'[`]a dgY'cZ gca Yh\]b['VYmcbX'k cfXg"' =b'h\]g'Wci fgY'mci 'k]``YI d`cfY'\ck 'Ufh]ghg'WfYUhY'a YUb]b[Z\`YI dYf]YbW'g']b dYfZcfa UbW'''GhU[]b['gWf]dhgžXYg][b]b['gWfbYgžXYj]g]b['UWf]cbg'-'mci '```YUfb'UVci hih\Y'dfcWfgcZ a U_]b['h\YUhfY'UbX'\ck 'hc'di himci f'ck b']XYUg']bhc'dfUWf]W'''H\]g']g'U'Zci bXUhJcbU'`Wci fgY']b'dYfZcfa UbW'UbX'dfcXi Wf]cb"'=icdYbg'i d'cddcfhi b]hJYg'Zcf'UWf]b['žX]fYWf]b['UbX'XYg]['bž'VUW_ghU[Y'dfcXi Wf]cbž'gWf]dh k f]hJb['UbX'fYj]Yk]b['IbX'Yy]fy |]h'a you'' a land a la

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- %" 8 YgWf]VY 'UbX ']bhYfdfYh'U'h\YUlfY 'Yj Ybh]b'hYfa g'cZ]hg'a i `h]d`Y'g][b]Zm]b['Y`Ya Ybhg'UbX'h\Y]f Wta d'Yl ']bhYfUWhcbg'i g]b['qYa]ch\WhYfa g'UbX'WtbW\dhg
- &" 5bU`mgY`fY`Uhjcbg\]dg`VYhk YYb`fUŁ'h\YUhfY`Yj Ybhgž'hYl hgždfUWhJWYg`UbX`h\Ycf]YgžUbX`fWŁ'h\Y]f qcWjU``UbX`\]qhcf]WU``WcbhYl hg
- ' " 8]gW ggž'Wca dufy 'UbX'WcblfUghth\Y'U]a g'UbX'UddfcUWXYg'hc'dYfZcfa UbWY'a U_]b['UbX'Ui X]YbWY fYWYdf]cb'cZ_YmdfUWf]r]cbYfg'UbX'h\Ycf]ghg']b'tk Ybh]Yh\!WYbh fmK YghYfb'h\YUhfY'UbX WcbhYa dcfUfmdYfZcfa UbWY
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-) " C dYfUhY YZYWhj Y`m]b h\Y`i b]j Yfg]lmYbj]fcba YbhUgʻUʻgY`Zla chj UhYXʻghi XYbhcZh\YUhYʻUbX dYfZcfa UbW

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5F HG % \$\cdots \]g 'U 'WcfY '@Y j Y '\%'H\YUlfY 'UbX'DYfZcfa UbW''Ghi X]Yg 'fHDG\cdots \for iZJa]']Uf]nY ghi XYbhg 'k]h\ 'h\fYg\c\'X'WcbW'dhg 'UbX'i gYZ\'\UbU'mt]\WU''hYfa g"'\didfcj]XYg 'h\Y'Vi]'X]b['V'c\W_g'Zcf'h\Y a U'cfz']bhfcXi \W]b['Z bXUa YbhU''_bck 'YX[Y 'UbX'g_]\'\g']b. 'dYfZcfa UbW' UbU'mg]g/\]ghcf]\WU''YggUmk f]h]b['cb'dYfZcfa UbW''dfU\W]h]cbYfg'UbX'd`Umg\W]dhg']b'\WcbhYl h'UbX'[fci d! XYj]gYX'fY\YUfgU''UbX'di V']\WdYfZcfa Ub\W''dfU\W]\W''

5F HG % \$ ']g'ghfi Whi fYX'Ug'U'Wca V]bUh]cb'cZU'k YY_`m`YWhi fY'UbX'U'k YY_`mhi hcf]U`k \YfY'X]gWi gg]cbž dfUWh]WY!VUgYX'UbX'ghi XYbh'YX''YUfb]b['dfcW/ggYg'hU_Y'd`UW/"'H\Y''YWhi fYg'UfY''fY`Uh]j Y`mhYUW\Yf!`YX UbX']bhfcXi WY'WcbW/dhg'Yl d`cfYX']b'dfUWh]WU`'hi hcf]U`g''H\Y'hi hcf]U`g'ZcghYf'g_]``g']b'gY`Z\X]fYWYX'UbX'[fci d! VUgYX'`YUfb]b['h\fci [\'U'gYf]Yg'cZghi XYbh'YX'fY\YUfgU`gž'W'`a]bUh]b[']b'U'dYfZcfa UbWY'dfYgYbhUh]cb Yj Ybh'

HYUWXYf! YX``YUfb]b[`UbX`ZUW]]hUh]cb. `H\Y`Wci fgY`Wcbj Ybcfz`hc[Yh\Yf`k]h\`]bj]hYX`[i Ygh`YWi fYfg`UbX hi hcfgz`k]```cZYf`hYUWXYf! YX``YUfb]b[`h\fci [\ci hih\Y`Wci fgY" @YWi fYg`UbX`hi hcf]U`g`k]``XYj Y`cd`mci f ZJa]`]Uf]hmk]h\`h\Y`gi VYWhUbX`dfcj]XY`U`Zci bXUh]cb`Zcf`Z fh\Yf`gh Xm" HYUWX]b[`ghUZk]```U`gc`ZUW]`]hUhY [fci d`dfYgYbhUh]cbg`Vmghi XYbhg"

; fci d!VUgYX'GY'Z18]fYWfYX'@YUfb]b['fG8@L'±b'dfYdUfUh]cb'Zcf'h\Y'; fci d'DfUWf]WU``DfcYWfighi XYbhg'k]``VY']bj c'j YX']b'a UbU[]b['[fci d!`YUfb]b['UbX'dfcV`Ya !gc'j]b['Vch\']b'UbX'ci hcZh\Y'k YY_miWci fgY'h]a Y g`ch''H\YfY']g'bc'fYei]fYX'fYUX]b['gYhZcf'h\YgY'`UghZci f'k YY_g"'±bghYUXž'dfYdUfUhcfmk cf_'k]``'Wcbg]ghcZ]bX]j]Xi U``fYgYUfW\ž'[fci d'a YYh]b[g'UbX#cf'[fci d'fY\YUfgU`g"

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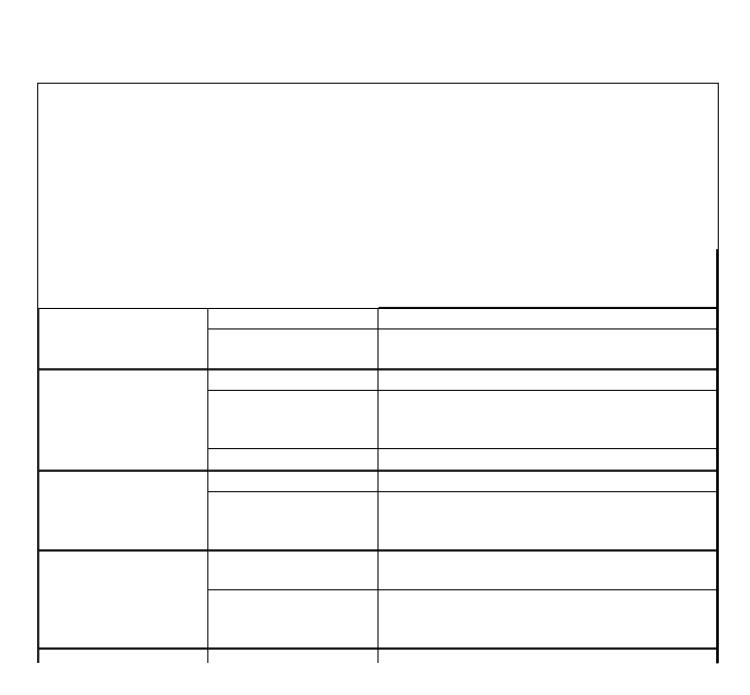
8 YHJ]`g. K f]hY`U`%\$\$\$!k cfX`UbU`mg]g`cZcbY`fYWYbhh\YUhY`Yj YbhflZca 'h\Y``]ghcZh\YUhY`Yj Ybhg`dfcj]XYX]b`WUgg\!"Fi Vf]W]bX]WUh]b[``Yj Y``cZdYfZcfa UbWY`U[U]bghYUW.`UggYgga YbhWf]hYf]Už'k f]hhYb`Zcfa Uh]j Y ZYXVUW_ž'UbX`dYfWYbhU[Y`[fUXY"

Hi fb]h]b gYh]b[. 'H\]g Ugg][ba Ybh]g gi Va]hhYX h\fci [\'Hi fb]h]b UbX gh XYbhg Xc bchgYY Hi fb]h]b g]a] Uf]hm

5ggYgga Ybh(. +bX]j]Xi U`7cbhf]Vi h]cb hc DfUWh]WU`Dfc YWh

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K YY_', . '* '5df]`'! '%\$'5df]`	@YWn fY	DfUWNW``DfcYWn—'FY\YUfgU`g"'FYj]Yk'fYgYUfW\" 6Y[]b'fY\YUfg]b[']b'mcif'U``cWUHYX'jYbiY"
	Hi lcf]U`	DfuWjWU``DfcYWi—'Wcbljbi Y'fY\YUfg]b["'DfYgYbh'UbUWjcb``]ghUbX'XYg][b'WcbWdhhc'mci f'Hi hcf/'A Uf_A]hWXY``"
	5ggYgga Ybh	9ggUmXi Yž'Hi YgXUnž'+'5df]``&\$&\$
K YY_''%' '5df]`'!'%+	@YWhi fY	Di V`]W\c`]XUm"Bc'`YWn fY"
5df]`	Hi lcf]U`	Dfuwjwu``Dfc'Ywi-'wcbijbi Y'fY\Yufgjb["'Ghu[Y'Udfcj]g]cbu``k U`_!h\fci [\'cZh\Y'dYfZcfa Ubw'f]nggYei Ybwgz'UffUb[Ya Ybng'Ubx'YZYwngt''DfYgYbhmci f'V`cw]b[#W.cfYc[fUd\m'nc'mci f'Hi hcf'Ubx'A Uf_A]hW.Y`"
K_YY_`%\$.`&\$`5df]``!`&(@YWhi fY	DfUWjWU``DfcYWi—'WcbljbiY'fY\YUfg]b["
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K YY_'‱'&+'5df]`'!'&, 5df]`	@YVVni fY	Dfuwhjwu``DfcYwh-'HYW\#XfYgg'FY\YUfgu``f1\$ a]bi hYg'VYhkYYb'- Ua!%daž'hc'VY'UXj]gYXŁ'UbX DYfZcfaUbW'`flYwhifY'g`chž&da!'.'\$da 'Ž'Vi ad!cih '\$'a]bi hYgt"
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hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'' =Zmci
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a i ghfYhU]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU``Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'' =Zmci 'Ya U]`'9! hYfbU``Gi ddcfhmci 'k]``

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'=hWUb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhU``mWcdm]b['Zfca `U`gci fW'k]h\ci hUW_bck `YX[Ya Ybh'

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b[`WUhY[cf]Yg.$

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

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