

HUMS1008

A i g]Wcb'A mA]bX. DgmWkc'c[mUbX'A i g]W

HYfa 'H\fYY''##'&\$&\$

7ci fgY'Cj Yfj]Yk

GHJZ:7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
8f [.] 5bh\cbm7\a]Y`	Ubh\cbm'W\a]Y`4 i bgk "YXi "Ui	,	K 65%*ž	
			FcVYfh	
			K YVghYf	
			6i]`X]b[

GWXcc~7cbhJWh~abZcfa Uhlcb

GWXcc`cZh\Y'5fhg'UbX'AYX]U

Fcca " %&ž@YjY`" žFcVYfhK YVghYf'6i]X]b['f) %(Ł

D\cbY.'f\$&Ł'-',)'(,)*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. k k k "Ufhg"i bgk "YXi "Ui #gUa

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck``YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubgž h\Y'6YXY[U'`fPYbg]b[tcb'WJadigŁZ'; UX][U'`fP]tmUbX'5fthZ''8Yg][b'7UadigYgŁUbX't\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cfW'5WJXYam]b'7UbVYffUŁ'cZh\Y'`UbXg'k\YfY'YUW\'WJadig'cZIBGK']g`cWJhYX''$

7ci fgY 8YHJ] g

7 fYX]hDc]bhg *

Gi a a UfmcZh\Y 7ci fgY

H\]g`Wci fgY`Ug_g`ei Ygh]cbg`UVci ha i g]WWc[b]h]cb`UbX`VY\Uj]ci f. `<ck `Xc`k Y`dYfWr]j Y`a i g]WB`K \m\Wb Ub`]bghfi a Ybhgci bX`a i g]WJ`3'<ck `Xc`k Y`fYgdcbX'hc`UbX'dfcWrgg'h\Y`gci bX3'K \Uh\UddYbg'k \Yb`k Y UfY'dfYdUf]b[`UbX'dYfZcfa]b[`a i g]WB`K \m\Wb'dYfZcfa Yfg`VYWca Y`XYV]`]hUh]b[`mbYfj ci g3'K \Uh]g`h\Y fY`Uh]cb`VYhk YYb`a i g]WZgYI `UbX'W\YYgYWJ_Y3'7 Ub`a i g]Wa U_Y`mci `ga UfhYfž'UbX`k \Uh]g`h\Y`A cnUfh 9ZZYWB`K \mXcYg`h\Uhh bY`[Yhghi W_]b`a m\YUX3'<ck `c`X`a i ghU'dYfgcb`VY`VYZcfY`h\YmWJb`\YUf`UbX UddfYW]UhY`a i g]WB`Nci `k]```UXXfYgg`h\YgY`UbX`fY`UhYX`ei Ygh]cbg`h\fci [\`YI Ua]bUh]cb`cZh\Y`a i g]W dgmW\c`c[m`]hYfUh fYz'UbX`h\Y`Wf]h]WJ``Yj U`i Uh]cb`cZmci f`ck b'a i g]WU``Uhhhi XYgz`VY`]YZg`UbX`VY\Uj]ci fg"

7 ci fgY @YUfb]b[Ci hWca Yg

%" 9I d`U]b`\ck 'a i g]W]g`XYZ]bYX`Z̄ca 'U'dgmW\c`c[]\W\`dc]bhcZj]Yk "
&" \(\text{XYbh]Zm\ck 'a i g]\Wdgm\\c`c[]\ghg`]\bj Ygh][UhY'ei Ygh]cbg'U\vci ha i g]\\\'
" F Y\\\c'[b]\gY'h\Y'gci f\\\'g'UbX'k Umg']\b'k \]\\\\ a i g]\\\dfc\\\'gg]\b[']\g'i b\XYfghccX\\\\'a dUfY'h\YgY k]h\'Zc` 'dam\\\\c`c[]\\\\\\'UbX']\bh ihi Y'i b\XYfghUbX]\b[q

HYUWX]b['GhfUhY[]Yq'

H\Y'Wti fgY'k]``VY'dfYgYbhYX'h\fci [\'ZJVW!hc!ZJWW'`YWfi fYg"'Hi hcf]U`g'UfY`\Y'X'cb`]bYž'k\]W\'a YUbg'mci g\ci 'X'YI dYWfihc'XYj chY'i d'hc'cbY'\ci f'dYf'k YY_'fbch]bWi X]b['dfYdUfUh]cb'UbX'UggYgga Ybhih]a YE'hc cb`]bY']bX]j]Xi U``UWfj]hJYg'UbX'Wc``UVcfUh]j Y'UWfj]hJYg'k]h\ ch\Yf'ghi XYbhg"'C h\Yf'UggYgga YbhihUg_g'k]``VY Wta d`YhYX']bXYdYbXYbhmi]b'UXX]hJcb'hc'h\Y'cb`]bY'hi hcf]U``k cf_"'; fci d``YUfb]b['zWf]hJWU``fYZYWfJcb'UbX'gY`Z UggYgga Ybhik]```VY'XYj Y`cdYX']b'gY`YWhYX'hi hcf]U``HUg_g'hc'YbWti fU[Y'X]j YfgY'a cXYg'cZ`YUfb]b[']b UXX]hJcb'hc'hfUX]hJcb'hc'hfUXJhJcb'hc'hfUXJg"

5ggYgga Ybh

5ggYgga Ybh'HUg_g

5ggYgga Ybh'hJg_		

8YHJ]`g.

 $H\Y'HYghUggYggYg''YWh fY'WcbhYbhbchUggYggYX']b'h\Y'Ei]n'''EiYgh]cbg'k]```dfcVY'VUg]WWcbWYdhg dfYgYbhYX']b'h\Y'WcifgY'WcbhYbhg''''H\Y'hYghk]``Wcbg]ghcZai'h]d'Y'W\c]WY'UbX'g\cfhUbgkYf']hYag''''$

: YYXVUW_`k]```Wcbg]ghcZU'bi a Yf]WU``a Uf_"'

5XX]h]cbU`XYhJ]`g.

GYY'AccX`Y'Zcf'Zfh\Yf'XYhU]`

FYgci fWyg

DfYgWf]VYX`F Ygci fWYg`

Bch'Uj U]`UV`Y

FYWca a YbXYX FYgci fWyg

Bch'Uj U]`UV`Y

7 ci fgY '9j U'i Uh]cb 'UbX '8Yj Y`cda Ybh

Gi Va]gg]cb cZ5ggYgga YbhHUg_g Hi fb]h]b Gi Va]gg]cb

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX'dfYgYbh]b['h\Ya 'Ug`mci f`ck b"'=h\Wb'hU_Y`a Ubm Zcfa qžZfca 'XY`]VYfUhY'W\YUh|b['hc`UWW]XYbhU`mWcdm]b['Zfca 'U'gci fW'k]h\ci h'UW_bck 'YX[Ya Ybh'

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'] Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`h\I hcf']XYU'k]h\ci hUW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U'gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfc'YWgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_jb['k]h\ 'ch\ Yfg'Vi h'dUgg]b['cZZh\ Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'hc'Ubch\ Yf'ghi XYbhVYZcfY'h\ Y 'Xi Y 'XUhYzcf'Zcf'h\ Y' di fdcgY'cZh\ Ya d`U[]Uf]g]b['Uh'Ubmh]a Yz'dUm]b['Ubch\ Yf'dYfgcb'hc'dYfZcfa 'Ub'UWUXYa]WhUg_z'ghYU']b['cf'UWei]f]b[Ubch\ Yf'dYfgcb'g' UWUXYa]Wk cf_'UbX'Wcdm]b[']hz'cZYf]b['hc'Wca d`YhY'Ubch\ Yf'dYfgcb'g' k cf_'cf'gYY_]b[dUma YbhZcf'Wca d`Yh]b['UWUXYa]Wk cf_"

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[ˈgci fW/gˈk \]WX`\Uj Y`bchVYYb`fYUXžk]h\ci hUW_bck`YX[]b[ˈh\Y`″gYWcbXUfm″gci fW/Zfca ik \]WX`_bck`YX[Y`cZh\Ya`\UgʻVYYb`cVhU]bYX"

8 i d`]\WUh]cb`ffgY`Zd`U[]\Uf]ga "Ł`gi Va]\h]b[`mci f`ck b`k cf_ž]b`k \c`Y`cf`]b`dUfhžk \YfY`]h\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\hYX`Zcf`Ubch\Yf`UggYgga Ybhcf\Wci fgY`UhI BGK `cf`Ubch\Yf`i b]j Yfg]\m'

7 cffYWhfYZYfYbWb[dfUWhWyg.

- DUfUd\fUq]b[žgi a a Uf]q]b[žYggUmk f]h]b['UbX'h]a Y'a UbU[Ya Ybh
- 5ddfcdf]UhY'i gY'cZUbX'Uhff]Vi h]cb'Zcf'U'fUb[Y'cZa UhYf]U`g']bWi X]b['hYl hž']a U[Ygž'Zcfa i `UY'UbX WbWYdhg"

±0X]j]Xi U``Ugg]ghUbWr`]g`Uj U]`UV`Y`cb`fYei YghZfca `H\Y`@YUfb]b[`7 YbhY`f\hd.#k k k "`Wi bgk "YXi "Ui #£" Ghi XYbhg`UfY`U`gc`fYa]bXYX`h\UhWUfYZ ``h]a Y`a UbU[Ya Ybh']g`Ub`]a dcfhUbhdUfhcZghi XmUbX`cbY`cZh\Y]XYbh]Z]YX`WUi gYg`cZd`U[]Uf]ga `]g`dccf`h]a Y`a UbU[Ya Ybh'`Ghi XYbhg`g\ci `X`U``ck `gi Z]W]Ybh'h]a Y`Zcf fYgYUfW\z`XfUZh]b[`UbX`dfcdYf`fYZYfYbW]b[`cZgci fWg`]b`dfYdUf]b[`U```UggYgga Ybh']hYa g"

IBGK @]VfUfmU`gc`\Ugʻh\Y`9@&9`hcc``UjU]`UV`Y`hc`Ugg]ghmci`k]h\`mcif`ghiXmUhIBGK"`9@&9`]g XYg][bYX`hc`]bHfcXiWY`bYk`ghiXYbhg`hc`ghiXm]b[`UhIBGK`Vih]hWUb'U`gc`VY`U`[fYUhfYZfYg\Yf`Xif]b[`mcif

- i bXYfghUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'ghi XYbh'Uhil BGK
 VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hžI BGK 'Ghi XYbh'7cXY'cZ7cbXi Wh'UbX'5WW'dhUV`Y'I gY'cZ I BGK '=7 H'F Ygci fWfg'Dc`]Wh

5 WUXYa]W + DZcfa Uh]cb

: cf'YggYbhJU`'ghi XYbhi]bZcfa UhJcb'fY`UhJb['hc.

- fYei Yghg Zcf Yl hYbg]cb/
- `UhY 'gi Va]gg]cbg '[i]XY `]bYg/
- fYj]Yk 'cZa Uf_g/
- I BGK '< YU'h\ 'UbX'GUZYhm'dc']W]Yg/
- YI Ua]bUh]cb dfcW/Xi fYg/
- •