

ARTS1190

GmXbYm'<]ghcfmž'@UbXgWUdYgž'DYcd`Y

HYfa 'H\fYY''##'&\$&\$

7ci fgY⁻Cj Yfj]Yk

GHJZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
>Ua Yg?YUHb[_ , . 5		A cfj Yb [·] 6fck b &, \$	

GWXcc``7cbHJWhʻ±bZcfa Uh]cb

GWkcc`cZ<iaUb]hJYg'UbX'@Ub[iU[Yg

@c\\U||cb. G\\cc``C\\Z|\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

CdYb]b['<ci fg. 'A cbXUm! ': f]XUmž'- Ua '!') da

D\cbY.'Ž*%'&'-',)'%*,%

: UI . 'Ž * %'&'-' ,) ', +\$)

9a U]`. \<u>\U`4 i bgk "YXi "Ui</u>

7ci fgY⁻8YHJ]`g

7fYX]hDc]bhg**

Gi a a UfmcZ'h\Y'7ci fgY

 $\label{thm:condition} $$H\]g'WcifgY']a\ a\ YfgYg'mci\]b'h\Y'\]ghcfmz'dc']h]Wg'UbX'W'h fY'cZGmXbYm'UbX'h\fci [\'h\Ya\ z']bhfcXi W'g'mci\]$

8YHJ]`g.

6]V`]c[fUd\mWca df]gYg`U``]ghcZ%\$`[ccX`ei U`]migci fWYg`Zcf`h\Y`a U^cf`dfc^YWf'`5Vci h) \$\$`k cfXg"

♣X]j]Xi U``ZYYXVUW_`Vmfi Vf]Wd`i g`bi a Yf]WU``[fUXY"

5XX]h]cbU`XYhU]`g.

H\]g`Ugg][ba Ybh]g`hc`a U_Y`gi fY`mci `UfY`k cf_]b[`hck UfXg`mci f`A U^cf`G]hY!VUgYX`dfc^YWhfUggYgga Ybh 'E`UbX`cb`hfUW_hc`Wca d`Yh]b[`]hhc`U`\][\`ghUbXUfX"``=b`]hžmci `k]``bYYX`hc`dfcj]XY.

- % 5 'gmbcdg]g#UVglfUWh 'H\]g']g'U'g\cfhfUVci h' \$\$ 'k cfXgž')!* 'gYbhYbW'gŁ'gi a a UfmidfYgYbh]b[mci f'cj YfU``'Uf[i a Ybhfh\Yg]gŁ'h\Uhmci 'k]``'VY'Uf[i]b[']b'mci f'a U'cf'dfc YWf''Mci 'k]``'ci h]bY'k\m mci f'W\cgY'g]hY']g'g][b]Z]WUbhž'k\Uh]h'hY`g'i g'UVci h'GmXbYm'UbX']hg'\]ghcfma cfY'[YbYfU``mž k\UhYj Ybhgž'h\Ya Ygž'dfcW'gg'mci 'ZYY`'h\Y'g]hY'a][\hfYdfYgYbhž'YhW''Mci 'k]``'U`gc'bYYX'hc'ci h]bY h\Y'UddfcUW\mci 'k]``'VY'hU_]b[']b'hYfa g'cZa Yh\cXgž'UfYUg'cZ'ZcW'g'fY''["ž'gcW]U''[fci dgž'\]ghcf]WU`dYf]cXg'YhW'''K f]h]b['h\]g'UVghfUWhk]``'\Y`d'mci 'hc'VY'WYUf'UbX'gi WW]bWhUVci hmci f'Uf[i a YbhUbX ZcW'g"
- &" 5 V]V`]c[fUd\mžWcbg]gh]b[cZ ' %" Df]a UfmGcifWYg. '5 `]ghcZU'a]b]a i a 'cZXagdgcifWYg'fa UhYf]U'ž'k f]thYbž'UfW.Yc`c[]\W\

±bX]j]Xi U`ZYYXVUW_Vmfi Vf]Wžk f]hhYb'Wca a Ybhd`i g'bi a Yf]WU`[fUXY"

5XX]h]cbU`XYhJ]`g.

 $\label{thm:continuous} $$H\g'UggYgga\YbhfYei\]fYg'hc'fYgYUfW.'UbX'k f]h'U'dfc'YWicb'Ub']a\ dcfhUbhid'UW'z'g]h'Cf'bY][\Vci f\ccX']b\ GmXbYm''H\]g']g'h\Y'a\ U'cf'd]YW'cZk cf_'Zcf'h\]g'Wci fgYz'UbX'k \YfY'mci 'WUb'XYa cbghfUhY'mci f'fYgYUfW\z'UbU'mj]WU'z'h\YcfYh]WU'UbX']bhYfdfYh]j Y'g_]``g''$

7\ccgY`CB9`cZh\Y`Zc``ck]b[`g]hYg`f]Zh\YfY`]g`gcaYk\YfY`Y`gY`mci`kci`X``]_Y`hc`kcf_`cbž'd`YUgY`YaU]`aY`]b`UXjUbW\`gc`h\Uh`=`WUb`UddfcjY`]hŁ

- FYXZYfb'fH\Y'6`cWŁ
- @U'DYfci gY
- A cfhi UfmGHUhjcb UbX#cf F cc_k ccX 7 Ya YhYfm
- < mXY DUf 6UffUW q
- H\Y'< mXY'DUf_'7 YbcHJd\
- A Uff]W_i]``Y
- 7 UVfUa UHU
- 7 i ghca g'< ci gY
- 6cHJb]W; UfXYbg
- AigYia cZGmXbYm
- 7cW_Uhcc'=g`UbX
- DUffUa Uhtu flygd" h, Y Wa Yhyfmt
- 6cbX]⁻6YUW
- ?]b[g'7fcgg
- 8 Uf]b[\ifgh; Uc`

Mci 'a i ghj]g]hh\Y'd`UWY'mci 'UfY'k f]hjb['UVci hžgc'mci f'fYgYUfW\'a i gh']bWi XY'Uh`YUghcbY'j]g]hhc'mci f g]hYfgŁ'cf'dUfhg'h\YfYcZ'' \(\dag{h} \)mci f'Ugg][ba Ybhž'mci 'a i gh']bWi XY'U'd\chc'cZmci fgY`ZUhh\Y'g]hY'hc'dfcj Y'h\Uh mci 'k YfY'h\YfY'''

Mci f'dfc YWng\ci X fbchbYWggUf] m]b h\]g cfXYfL

- 8 Y g W f] V Y 'h \ Y 'g] h Y /
- Cih]bY'h\Y'\]ghcfmcZh\Y'g]hYž'gYhk]h\]b'k]XYf'\]ghcf]WU''WcbhYI hg'UbX'h\Ya Yg/
- 9I d`cfY`k\Uhih\Y`g]ihY`hY``g`i g`UVci hih\Y`dYf]cX`]b`k\]W\`]hik Ug`Vi]`hcf`WfYUhYXž`UbX`k\Uhi]hihY``g`i g
 UVci hih\Y`\]ghcfmcZh\Y`Wjmicj YfU``"'H\]g`Wca dcbYbhU``ck g`mci hc`XYj Y`cd`Wf]hJWU``UbX`UbU`mhJWU`
 ei Ygh]cbg`UVci himci f`g]hY/

•

a UHYf]U`Zcf'g]HYg'k]``j Ufmž'Vi h'V]V`]c[fUd\]Yg'g\ci `X'WcbHJ]b'U'a]b]a i a 'cZY][\higi VgHJbH]U``fYZYfYbWYg"

 $\label{thm:condition} $$HY''i gY'cZgca Y'df]a Ufmigci fW'g']g'glfcb[`mYbWci fU[YX'!'k Y'k]``X]gW'gg'\ck 'hc'fYUX'UbX'UbU'mgY h\YgY'cj Yf'h\Y'Wci fgY'cZh\Y'hYfa "$

 $\label{thm:continuous} \begin{tabular}{ll} Hi fb]h]b gYhh]b[. H\]g Ugg][ba Ybh]g gi Va]hhYX hAfci [\Thi fb]h]b UbX gh XYbhg WUb gYY Hi fb]h]b g]a] Uf]hm fYdcfhg"$

5 hm/b XUb VW F Yei]fYa Ybhg

 $\hbox{Ghi XYbhg'UfY'ghfcb[`mYbWci fU[YX'hc'UhhYbX'U```WUggYg'UbX'fYj]Yk ``YWhi fY'fYWcfX]b[g''] }$

7ci fgY GWX YXi `Y

J]Yk 'WUgg'hja YhUV'Y

H]a YtUV`Y

8 UhY	HmdY	7 cbhYbh
K YY_'%'%('GYdhYa VYf'!	@YWnifY	7 cifgY`±olfcXiWfjcb. 7 cbj]WhiHck b hc; `cVU`7]hm
% 'GYdhYa VYf	GYa]bUf	±blfcXi Whjcb. K \Uhjg Mci f'GmXbYm3
K YY_'&.'&%'GYdhYa VYf'!	@YWn fY	Cb`]bY`@YWfifY.`5Vcf][]bU``@UbXgWUdYg`cZGmXbYm
&) GYdhYa VYf	GYa]bUf	; cj Yfbcf'D\]``]d'UbX'h\Y'9cfU'BUh]cb
K YY_" . &, "GYdhYa VYf"! &"C WcVYf	:]Y`Xk cf_	91 d`cf]b['h\Y'7 cbj]WhgfiHck b
		D`YUgY`Xck b`cUX`f\Y`I BGK 'K U`_]b[`Hcif/Zcf`f\Y "9Id`cf]b[`7 cbj]WfGmXbYm´'fcifžigY`f\Y`Wcidcb WcXY.`6 < G&HG`UbX`f\Y`UVWcibfYaU]`. \U`4 ibgk "YXi"Ui"
		@schY."h\]g"hU_Yg"h\Y"d`UWY"cZmcif"`YWhifY"h\]g"kYY_0
	GYa]bUf	7 cbj]WnG`i a gʻcfʻH\f]j]b[ˈBY][\Vci f\ccXg3
K YY_'(.') 'C WcVYf'!'- C WcVYf	@YWn fY	Cb`]bY'@YWfifY.'6cca '7]lmž; YbXYfYX'7]lm
	GYa]bUf	K ca YbfgʻD`UWY`]bʻh\Y`7]hm
K YY_').'%&'CWfcVYf'!'%* CWfcVYf	5ggYgga Ybh	A U^cf`9ggUmUbX`6]V`]c[fUd\mXiY`:f]XUm %*`CW\cVYf"`
	@YWh fY	Cb`]bY'@YWhifY.'F]W\'GmXbYmž'Dccf'GmXbYm
	GWfYYb]b[D`YUgY`k UHW\`fD`Um b[`]b`H\Y`G\UXck gfif&\$\$, Ł`]b mci f`ck b`Ha Y`f1]b_`Uj U]`UV`Y`H\fci [\`A ccX`YŁ
	C b`]bY'5Wfjj]hm	

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

 $5 ```Wci fgY'fYUX]b[g'k]```VY'Uj U]`UV'Y'cb'A ccX'Y'j]U'@Y[Ubhc'Ž'UXX]h]cbU``a UhYf]U``Zcf'X]gW gg]cb'`]b gYa]bUfg#cZ]bhYfYgh'Zcf'Ugg][ba Ybhg'k]```VY'dcghYX'kYY_`m''$

FYWca a YbXYX FYgci fWYg

B#5

7 ci fgY '9j U'i Uh]cb 'UbX '8Yj Y`cda Ybh

 $H\[g^{g}\]g^{h}\Y^{g}YWcbX^{h}\]aY^{h}\[g^{i}\ b]h^{i}\]g^{v}Y]b[^{h}Ui\ [^{h}z^{i}\]g^{h}Y^{u}U[Yf^{h}c^{h}fYW^{h}]jY^{h}mcif^{h}z^{h}YXVUW_{j}^{u}]U$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bž'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-',) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'Y! hy'bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hy'Yd\cby'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cby''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWhg'cZ9@&9'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'Uh'l BGK "'\\hd.##gi V'YWfi |XYg"`]VfUfm'i bgk "YXi "Ui #\`]qY#JVci hY`]qY