

# **ARTS2876**

I bXYfghJbX]b[ 'h\Y'GY`Z

HYfa 'C bY''##'&\$&\$

## 7ci fgY<sup>\*</sup>Cj Yfj ]Yk

### <sup>'</sup>GhJZ'7cbhJWh'8YhJ]`g'

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWUh]cb	D∖cbY
AY`Ub]Y`K\]HY		K YXbYgXUmg %Ua!&da'UbX H\ifgXUmg %Ua!&dažcfVm Uddc]bhaYbh	A 6%*'	- ' , ) '&' \$(

### 'Hi hcfg'

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWJhjcb	D\cbY
1 -	f"a WUi f]b!ga ]h\4 i bgk "YXi "Ui	H68	H68	H68
A W@Ui f]b!Ga ]h∖				

### GWXcc`7cbHJWhi±bZcfa Uhjcb

GWkcc``cZGcWJU``GWJYbWYg

Fcca '%) -

A cfj Yb 6fck b 7 &\$

Ya U]`. 'gcgg4 i bgk "YXi "Ui

d\cbY. '\$&'-',) '% \$+

## 7ci fgY 8YHJ] g

7 fYX]hDc]bhg\*\*

Gi a a UfmcZh\Y 7ci fgY

 $9 \ UW.\ cZi\ g`\ Ug`\ UgYZUbX`\ Ub']XYbh]mVmj\ ]fhi\ Y`cZVY]b[\ ``i\ a\ Ub''``6i\ hXc`ch`\Yf``]j\ ]b[\ `VY]b[\ g`\ Uj\ Y`UgYZ3\\ 8 \ c`ch`\Yf``]j\ ]b[\ `VY]b[\ g`\ Uj\ Y`gcW]Yhm]b`h`\Y`gUa\ Y`k\ Um`\i\ a\ Ubg`Xc3``\=b`h`]g`Wci\ fgYz`mci\ k\ ]```Wcbg]XYf`gca\ Y\ hfUX]h]cbU``Uggi\ a\ dh]cbg`cZgY`\\ccX`fY''[\ "z`h\Y`WUdUW]hmZcf`fYUgcbz`gdYYW.z`UbX`a\ Ya\ cfmz`Zca\ 'U`fUb[\ Y`cZ\ AccX`fY'']$ 

 $\label{thm:condition} Hi hcf] U`g`k ]```VY`i gYX`hc`cf[Ub]gY`ga U```[fci dg`hc`YghUV`]g\`U`Wc``UVcfUhj Y`k cf_]b[Ybj]fcba Ybhk \YfY`gh XYbhg`WUb``YUfb`Zfca `cbY`Ubch\Yf''`$ 

 $FYUX]b[\ 'E' i Ygh]cbg. ': cf'YUW' k YY_mfYUX]b[\ \check{z}'mci' k\ ]```Z]bX'fYUX]b[\ 'Wca dfY\Ybg]cb'ei Ygh]cbg'dcghYX'hch\Y'I b]j Yfg]hm@A G''H\YgY'k ]```\Y`d'hc'cf]Ybh'mci' k ]h\'fYgdYWh'c'h\Y'Uf[i a Ybhg'dfYgYbh'X']b'h\YUgg][bYX'fYUX]b[g''$ 

## 5ggYgga Ybh

### 5ggYgga Ybh'HUg\_g'

5ggYgga Ybh'HJg_	K Y][ \h	8i Y'8UHY	Gh XYbh@YUfb]b[ Ci hWca Yg 5ggYggYX
K cf_Vcc_	) \$1	- "A UfWX 'fK YY_g''&'/ " \	&Ž
; fci d': UWj^]HUH]cb'	&\$ı	K YY_g'(ž')ž'+ž', 'UbX'-	%Z
9ggUmi	' \$1	%"A Um'&\$&\$"Uh'%%) - "d"a "	%ž&ž(

### 5ggYgga Ybh'8YHJ]`g

5ggYgga Ybh% K cf\_Vcc\_

GhUfh'XUhY.

@Yb[h\. 5ddfcl]a UhY`m') \$\$ k cfXg dYf k YY\_

#### 5XX]h]cbU`XYhU]`g.

Mci 'k ]```gi Va ]hmci f`k cf\_Vcc\_`Ybhf]Yg`Zcf`K YY\_g`&`UbX`' 'cb`- '**A UfWX '&\$&\$**`Zcf`[ fUXYX`ZYYXVUW\_"

5ggYgga Ybh' . '9ggUm

GhUfh XUhY.

@Yb[ h\. '%) \$\$ k cfXg

 $8\ YhU]`g. `Ghi XYbhg`k ]```k f]hY`Ub`YggUmf%) $$`k cfXgŁ`h\UhfYZYV%g`cb`&!' `Wf]h]wU```YUfb]b[ `YI dYf]YbWYg`]b fY`Uh]cb`hc`Wci fgY`WcbhYbh'H\]g`]g`h\Y`Z]bU``UggYgga Ybh]b`h\Y`Wci fgY'': YYXVUW_. `K f]hHYb`Wca a Ybhg`UbX [ fUXYX`U[ U]bghU`Wf]hYf]U`g\YYh'`$ 

5XX]h]cbU`XYHJ]`g.

H\Y YggUm]g Xi Y cb %A Um&\$&\$ Uh %%) - d"a "

 $\label{thm:continuous} \begin{tabular}{ll} Hi & fb & fb & gYM &$ 

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		EWWUfW I d[f[`Yež'&bX'9X]h]cb"'CIZcfX.'CIZcfX
	11: 1 £1115	
K YY_'*.'&' 'A UfW\'!'&+ A UfW\	Hi hcf]U` Cb`]bY'5WIj ]hm	; fci d`: UWj`]hUh]cbg`Wcbh]bi Y`h\]g`k YY_" : `YI ]V]`]hmK YY_^`H\YfY`UfY`bc`gW\YXi `YX `YWhi fYg`cf`hi hcf]U`g`h\]g`k YY_"
		±b``]Yi 'cZ`YWi fY#i hcf]U`ž'd`YUgY`Wca d`YhY'h\]g cb`]bY`UWijj ]hmfgYY`A ccX`Y`Zcf`XYhU]`gŁ"
	FYUX]b[	flcf'Cb`]bY'5Whjj]hmz'
		7 cYmYYž'>"A "'f% Ł'H\Y'D\]`cgcd\Yfg'UbX'h\Y 5 b]a U`g'`]b 'HZWFS`` Wd>WUfgdWe a`: g_S` HS'gWe" 8 Y`]j YfYX'Uh'Df]bWhcb'l b]j Yfg]lmž'C WcVYf'%) ž % - +"'Dd"%%'!%('"
		? UZ_Už': fUbn'f% +%'''5 F Ydcfhhc'Ub'5WUXYa m' Dd"&) \$!&) - ']b'8c6` I =SX] S, FZW5a_ b'WfWEfaqWe'' BYk 'Mcf'GW\cW_Yb'6cc_g
K YY_`+.'' \$`A UfWX`!'' 5df]`	@YWhi fY	H\Y`5b]a U``UbX`h\Y`GY`Z'!`8YgWUfhYgž 8Yff]XU`f5df]``&Ł
	FYUX]b[	8 YgWJfhYgžF YbY fl/b-,, Ł'8 ]gWti fgY C b H\Y A Yh\cX  - DUfhJ 'Dd" (\$!(* '=b 6 WeUSdWe, E WWUfWW  B Z ['aeabZ [US^I d[f[ Ye fHfUbg" >c\b 7 chjb[ \Ua 5 bX F c VYfhGhcch\cZZL" 7 Ua Vf]X[ Y. 7 Ua Vf]X[ Y  I b]j Yfg]hmDfYgg"
		8Yff]XUž>UWeiYgʻf&\$\$(EʻJ]ciYbYʻf%-,,Eʻ8]gWcifgYʻCbʻH

	8Yff]XUž>UWeiYg`f(%+(&\$\$(Ł'H\Y`5b]aU``H\Uh H\YfYZcfY`=5a`fAcfY`Hc':c``ckŁ'=b`AUhh\Yk 7U`UfWc'5bX`DYhYf'5hhYfhcb`f9Xg"Ł'3`[_S^ BZ['aeabZk

### FYgci fWyg

#### DfYgWf]VYX F Ygci fWYg

 $Df]bhWcd]Yg`cZhY'k YY\_mUgg][bYX`fYUX]b[g`\Uj Y`VYYb`Wcad]YX`]bhc`Ub`f&FHG\&, +*`Ghi Xm?]hfik \]WX`]gUj U]`UV`Y`Zcf`di fWXUgY`Uhh\Y`I BGK `6cc_g\cd"``9`YWfcb]WWcd]Yg`cZh\Y`fYUX]b[g`UfY`U`gc`Uj U]`UV`Y`cb h\Y`5FHG&, +*`A ccX`Y`dU[Y.`\hd.#\acx`Y"hY`h'i bgk "YXi "Ui$ 

#### .

#### FYWca a YbXYX FYgci fW/g

### 7 ci fgY 9j U'i Uh]cb UbX 8 Yj Y'cda Ybh

Ghi XYbhiZYXVUW\_k]``VY`[Uh\YfYX'h\fci [\a m9| dYf]YbWY`gi fj YmgžUbX`mci `k]``VY`[]j Yb`cddcfhi b]hjYg h\fci [\ci h'h\Y`gYa YghYf`hc`[]j Y`]bZcfa U``ZYYXVUW\_"'H\Y``Ughihja Y`=HUi [\h3DFE\$\*)(G` VWdefS` V[Y fZW EWXk Ug`]b`&\$% "'H\]g`Wc\cfhcZghi XYbhg`[Uj Y`dcg]hj Y`ZYYXVUW\_cb'h\Y`Wci fgY"

%"'7 cbh/bh! '=\Uj Y'a cX]ZYX'h\Y'Wcbh/bh]b'cfXYf'hc'df]j ]'Y[Y'XYdh\'fUh\Yf'h\Ub'VfYUXh\'[]j Yb'h\Y dfYggi fYg'cZh\Y'hf]a Ygh/f'gmgh/a /

&"'5bbci bW'a Ybhg'!'=k]``i d`cUX'j ]XYc'gY[a Ybhg'hc'A ccX`Y']b'cfXYf'hc'UXXfYgg']ggi Yg'fY`UhYX'hc UggYgga Ybh'UbX'Wci fgY'Vi g]bYgg"'H\]g'k]``[]j Y'i g'a cfY'hJa Y']b'\$

#### Gi Va |gg|cb cZ5ggYgga YbhHUg\_g

### Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

Image: Ybwb: bh/f'u'dfcv'ya k \yb'uhh/a dh/b[ 'hc'gi va ]hmci f'ugg][ ba Ybhh\fci [ \ 'Hi fb]h/bž'd'YugY

HY'Yd\cbY'9| h/fbu''Gi ddcfhcb'-', ) '' ' ' %cf'Ya U] 'h\Ya 'cb'Y! h/fbu'h/hgi ddcfh4 i bgk "YXi "Ui "'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'\\$\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ'' Image
UfY'i bUV'Y'hc'gi va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\ 'Hi fb]h/b'mci 'a UmUdd'mZcf'Ub'Y! h/bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h/W\_Yhbi a VYf'Zfca '9! h/fbU''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'YY] UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj ]XYbW''hc'gi ddcfhmci f'Y! h/bg]cb'Udd']\WJh/jcb'' Image 'Ya U]''9! h/fbU''Gi ddcfhmci 'k ]'`
Ui hca Uh/WJ'`mfYW']j Y'U'h/W\_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k ]'`'bYYX'hc'gdYW/ZWJ'`mUg\_'Zcf'cbY''
Hi fb]h/b'U'gc'dfcj ]XYg'i dXUh/g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk ]hYf''

; YbYfU``mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\W)``mj ]U'Y]h\Yf'Hi fb]hjb'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]``'VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\ U`hYfbUhj Y'gi Va ]gg]cb'XYHJ]`g''

cfi]bZcfa Uh]cbicbi\ckihcigi Va ]hUgg][ ba Ybhgicbi]bYij ]UiA ccXiY.i\hdg.#gh XYbh'i bgk "YXi "Ui #\ck! qi Va ]hUgq][ ba Ybha ccXiY

#### 5 WUXYa | W < cbYghmUbX D`U[ | Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU\_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hUW\_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b[ 'WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW\_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf\_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k\YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b[ 'U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b[ 'h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k ]h\ci hUW\_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k ]h\ci hWfYX]hUbX'hc d]YW]b[ 'hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b[ "

7 c``i g]cb. 'k cf\_]b[ 'k ]th 'cth Yfg'Vi hidUgg]b[ 'cZZth Y 'k cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7 c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b[ 'mci f'k cf\_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

## 5 WUXYa ]W±bZcfa Uhjcb

: cf'YggYbhJU`gh XYbh]bZcfa UhJcb'fY`UhJb['hc.

• fYei YghgʻZcfʻYl hYbg]cb/