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+"'FYWc[b]gY'UbX'UddfU]gY'h\Y'ZJWcfg'Wcbff]Vi hjb['hc'gUZ/hm/'f]g_a UbU[Ya Ybh']ggi Yg']b'gdYW]ZJWa]b]b[!fY`UhYX'dfcWYggYg	D9%") ž'D9%"* ž'D9&"'
, "'±oj Ygh][UhY'h\Y'WUi gYg'UbX'WcbgYei YbWYg'cZa]b]b[!fY`UhYX gYf]ci g']bW]XYbhg'UbX'dfcdcgY'f]g_'a UbU[Ya YbhghfUhY[]Yg	D9%") ž'D9&"%ž'D9' "%
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